

مباراة الدخول 2020 - 2021

مسابقة في الرياضيات

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المدة: ٤٥ دقيقة

For each question, circle the correct answer. (Only one answer is correct)

1) Let  $f$  be the function defined by:  $f(x) = \ln(x^2 + 5x + 6)$ . The domain of  $f$  is :

- a)  $]-\infty; -3] \cup [-2; +\infty[$       b)  $]-3; -2[$       c)  $]-2; 1[$       d)  $]-\infty; -3[ \cup ]-2; +\infty[$

2) Let  $f$  be the function defined by:  $f(x) = \ln\left(\frac{e^x+1}{2e^x+3}\right)$ . Then  $\lim_{x \rightarrow +\infty} f(x) =$

- a)  $-\ln 2$       b)  $\ln 2$       c)  $-\ln 3$       d)  $\ln 3$

3) The derivative of  $f(x) = e^x - \frac{2e^x}{x+1}$  is:

- a)  $-e^x$       b)  $\frac{(x^2+1)e^x}{(x+1)^2}$       c)  $e^x - \frac{2e^x}{(x+1)^2}$       d)  $e^x - \frac{1}{(x+1)^2}$

4)  $\int \left( e^{5x} - \frac{1}{x} \right) dx =$

- a)  $\frac{1}{5}e^{5x} - \ln|x| + C$       b)  $5e^{5x} - \ln|x| + C$       c)  $\frac{1}{5}e^{5x} - x^{-2} + C$       d)  $\frac{1}{5}e^{5x} - (\ln x)^2 + C$

5) Let  $f$  be the function defined by:  $f(x) = \ln x + e^{-x}$ . The equation of the tangent to the curve of  $f$  at the point of abscissa 1 is:

- a)  $y = e^{-1}x + 2e^{-1}$       b)  $y = (1 - e^{-1})x + 2e^{-1} - 1$   
c)  $y = (1 - e^{-1})x - 1$       d)  $y = (1 - e^{-1})x + 2e^{-1}$

6) Let  $f(x) = \frac{e^x}{e^x - 1}$ . Then the curve of  $f$  admits:

- a) 0 asymptote      b) 1 asymptote      c) 2 asymptotes      d) 3 asymptotes.

7) Let  $f$  be the function defined by:  $f(x) = a(\ln x) - x$ , where  $a > 0$ . Then the function  $f$  admits:

- a) a local minimum at the point of abscissa  $a$ .      b) a local minimum at the point of abscissa  $1/a$ .  
c) a local maximum at the point of abscissa  $a$ .      d) a local maximum at the point of abscissa  $1/a$ .

8) Let  $f$  be the function defined by:  $f(x) = 2x - e^{-x} + 2$ . Then the function  $f$ :

- a) is strictly increasing over  $\mathbb{R}$ .      b) is strictly decreasing over  $\mathbb{R}$ .  
c) admits a local minimum.      d) admits a local maximum.

9) Let  $f$  be the function defined by:  $f(x) = \frac{1+x}{x^2+2x+5}$ . An antiderivative of  $f$  is:

- a)  $\frac{\frac{1}{2}x^2+x}{\frac{1}{3}x^3+x^2+5x}$       b)  $\frac{1}{2}\ln(x^2 + 2x + 5)$       c)  $\ln(x^2 + 2x + 5)$       d)  $\frac{1}{2x+2}$

10) The function  $f(x) = x^2 - 3e^{-x} + \ln(x+1)$  admits a root  $\alpha$ . Then  $\alpha \in$

- a)  $]0,6 ; 0,7 [$       b)  $]0,7 ; 0,8 [$       c)  $]0,8 ; 0,9 [$       d)  $]0,9 ; 1[$